

# 1     **Design of prototype dual axis tracker solar panel controlled** 2                                    **by geared dc servo motors**

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## 10    **Abstract:**

11                    Sunlight sensing for maximum illumination, providing initial position and delays  
12    of PV panel, design of an adequate control unit for minimal consuming servo motors are  
13    the main challenges of solar tracking systems. That is the objective of this paper to  
14    design and implement an automatic control for directing maximum solar illumination to  
15    a photovoltaic (PV) panel. The proposed prototype dual axis solar tracker panel is used  
16    to optimize the conversion of solar energy into electricity by orienting the panel toward  
17    the real position of the sun, at a cost of mechanical complexity and maintenance need,  
18    for the best efficiency. In hardware development, two geared DC servo motors are pulse  
19    width modulation (PWM) controlled by a drive unit moving the panel using four light  
20    dependant resistors (LDR) to provide analog signals processed by a simple and low  
21    energy ATMEGA328P microcontroller with Arduino. For the software part, after data  
22    processing, a C++ programming controls two DC servo motors to position light sensors  
23    in the most favorable direction, where solar panel and sensors will be perpendicular to  
24    the sunlight.

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25 **Keywords:** Arduino uno; dual axis; light dependant resistor; low cost solar tracker  
26 PWM control

## 27 **1. Introduction**

28       Regarding continuous depletion and pollution by using fossil fuels (oil, natural  
29 gas, coal...), thermonuclear (Uranium, plutonium...) and the increasing demand for  
30 energy during last forty years, researchers over the world try to develop new  
31 technologies to produce clean electrical renewable energy (REn) sources, so as solar  
32 and wind energy, considered as inexhaustible resources. Solar rays produced everyday  
33 to our planet is equivalent to million times consumption of the humanity global  
34 electrical need of energy. Solar energy is abundant, non-polluting, silent, reliable, free,  
35 and inexhaustible, need very low maintenance. For this reason, solar energy will be the  
36 most used to produce clean electricity.

37       Solar trackers are devices that orient solar panels, Fresnel reflector, mirrors or  
38 lenses towards the sun to receive maximum radiation as light and heat to be converted  
39 to thermal energy or to produce electricity. In 1839, the French physicist Alexandre-  
40 Edmond Becquerel was the first researcher who discovers that sunlight could be  
41 transformed into electricity. It is the photovoltaic (PV) effect. One century later, the first  
42 PV cells where constructed. The early solar modules were used in space in 1958. Other  
43 emerging technologies using multi-junction cells are concentrator photovoltaic (CPV)  
44 and concentrated solar power (CSP) which must use trackers to be pointed at the sun  
45 unless no energy will be produced. For these reasons, researchers are interested to  
46 motorize solar trackers. Mechanical and electrical are the main types of sun trackers. In  
47 1962, Finster introduced the first purely mechanical tracker [1]. In 1963, Saavedra  
48 designed an automatic electronic control mechanism [2]. After that, several works have  
49 been carried out on the design of single and dual solar tracking systems using

50 electromechanical actuators to allow about 30% to 60% more produced energy than  
51 fixed system because sunlight remains perpendicular to the PV panels [3-8]. Then, for  
52 improving the efficiency of PV conversion, we can use single or dual axis solar tracking  
53 [9-18], the optimization of solar cell configuration and geometry, new materials and  
54 technologies for optoelectronic applications etc...[19-22]. Although, solar trackers can  
55 gain more energy, some problems appear in their installation such as energy  
56 consumption, cost, reliability and maintenance. It is not recommended to use solar  
57 tracker for small panels because of high energy losses in the driving systems. We show  
58 that very low power consumption is 2 to 3% of the increased energy by tracking device.

59 The strategic choice of Algeria, a country of Northern Africa on the  
60 Mediterranean coast which ranges in latitude from *18.96* to *37.09* north and in longitude  
61 from *8.69* west to *11.95* east, is motivated by one of the most important potential solar  
62 for renewable energy in the world, recovered from sunlight reaching *3900 h*,  
63 particularly in the Sahara desert. A solar radiation Algerian map demonstrates solar  
64 energy potentials of specific zone to provide useful information for optimum plant  
65 selection of solar energy system [23]. This map can be used as database for future  
66 investments in solar energy showing that the highest intensity is around the area of  
67 Djanet (southern Algerian desert) and the less intense area is around Ksar Chellala  
68 (Tiaret High Planes).

69 In 2007, the first hybrid plant in the world constructed is located in Hassi R'Mel  
70 in southern Algerian desert. It is an ISCC (Integrated Solar Combined Cycle) composed  
71 of a conventional combined cycle and a solar field with a nominal thermal power of *150*  
72 MW. The goal of this project was to integrate the solar thermal technology in a  
73 conventional power plant which integrate a solar field of CCP (parabolic trough  
74 collector) covering a reflective area of *180 000 m<sup>2</sup>*. This combined use, reduces the cost

75 and facilitates the deployment of renewable energies in new industrializing countries.  
76 The power plant will be constructed in Boughezoul, on the northern edge of the Sahara  
77 desert (Aures), and will serve primarily as a pilot and research facility. It will be able to  
78 operate using just solar energy or as hybrid power plant fuelled by a combination of  
79 solar power and gas.

80 Algeria is engaged in a new age of sustainable energy use [24]. The program  
81 consists of installing up to 22 GW of power generating capacity from renewable sources  
82 between 2011 and 2030, of which 12 GW will be intended to meet the  
83 domestic electricity demand and 10 GW destined for export. This last option depends on  
84 the availability of a demand that is ensured on the long term by reliable partners as well  
85 as on attractive external funding. It is expected that about 40% of electricity produced  
86 for domestic consumption will be from renewable energy sources by 2030. This  
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89 In this context, this paper involves design and control of the prototype of a dual  
90 axis solar tracking system for solar PV panel to improve energy efficiency. Tracking  
91 system for solar PV panel improves extraction of maximum solar energy. The system is  
92 composed of two basic parts, the mechanical assembly and the electrical parts design.  
93 The electric part is composed of four identical LDR as the input, the ATMEGA  
94 microcontroller as the controller and two servo motors form the output.

## 95 **2. Solar Tracker Panels**

96 Taking into account geographic situation in Africa, Algeria disposes one of the  
97 most important sunny capacities in the world with 2200 KWh/m<sup>2</sup>/annum. The insolation  
98 on the most areas of the annual national territories reaches 2000 hours and could reach  
99 3900 hours in the Sahara. Daily received energy on a horizontal area of 1m<sup>2</sup> is nearly 5

100 *KWh* on the major zones, *1700 KWh/m<sup>2</sup>/annum* on the northern side and *2263*  
101 *KWh/m<sup>2</sup>/annum* on the southern side of the country [24-27]. Sunny capacities exceed  
102 *5000 TWh*. Table 1 shows the solar potential in three principal zones (coast zone, high  
103 planes, sahara) of Algerian territory.

104 Solar trackers represented in Fig. 1 are a field of PV panels mounted on a  
105 moving surface following the trajectory of the sun using dual axis trackers. Using a  
106 single axis, the panels could be installed in an inclined plan with a fixed angle on  
107 vertical pylon which will orient the PV field in the direction of the sun along the sunny  
108 day. The single axis panel could be as well on the same plan of the inclined panels  
109 which will be tipping from east to west in the direction of the sun. Dual axis solar  
110 tracker is mechanically more complex leaving the plan of the PV panels always in the  
111 perpendicular direction to the sun for any position in the sky.

112 The basic specifications which differentiate the trackers compared to stationary  
113 ones are the electrical production gain, orientation mono or multi axial, robustness  
114 (against wind) and reliability, and cost.

115 Using a dual axis solar tracker, the PV modules produces up to *40 %* of energy  
116 per annum with difference of production more significant (*>5times*) in higher  
117 consuming electrical energy hours at a cost of mechanical complexity and maintenance  
118 need [5].

### 119 **3. Moving PV Panels Interest**

120 Two basic most used solar PV panels are the single axis and dual axis trackers.  
121 Single axis tracker can either have a horizontal or a vertical axis. The dual axis solar PV  
122 panel tracker is characterized by the capability to move in both horizontal and vertical  
123 directions. The vertical and horizontal motion of the panel is obtained by taking altitude  
124 angle and azimuth angle as reference making them able to track the sun apparent motion

125 anywhere in the world throughout the day at any seasons. Furthermore, during seasonal  
126 changes, latitudinal sun offset must be compensated.

127 During the day, the sun is moving continuously; contrary to the fixed position  
128 PV generator that loses an enormous quantity of energy. To optimise the efficiency, the  
129 panels will be installed in the Algerian south area (Sahara). The energy collected by PV  
130 panels is maximal only at mid day as seen in Fig. 2. For this reason, if the PV panels are  
131 continuously oriented towards the sun, the maximal power will be provided for a long  
132 period of the day.

133 During a sunny day, *one kWp* system well oriented provides *5.5 kWh* of energy.  
134 The same tracker system, in the same sunny conditions, provides *11 kWh*. Fig. 2  
135 illustrates comparison of their production [5].

#### 136 **4. Methodology and technique of PV Panels**

137 This project consists on designing a dual axis tracker solar panel prototype,  
138 controlled by geared dc servo motors and analysing its working. It is composed of three  
139 main parts which are four LDR forming the inputs, the Arduino Uno as the  
140 ATMEGA328P microcontroller and two servo motors as the outputs where the block  
141 diagram is represented in Fig. 3. Analog signals from the cadmium sulfide LDR are  
142 captured by the ATMEGA328P converted to digital signals by Analog/Digital  
143 converters, adjusted by two potentiometers ( $R_{TOL}$ ,  $R_{VIT}$ ) and sent to two PWM  
144 controlled servo motors to move panel towards the sun rays.

145 Fig. 4 shows LM 7805 positive voltage regulator providing  $+5V$  required by the  
146 microcontroller and most of components of our realization.

147 The system is designed in two basic parts, the mechanical and the electrical.

#### 148 **4.1 Different components of the electric design**

149 In this section, we are basically interested to components of the solar tracker to

150 orient panel towards solar rays. The components of the hardware design are four LDR,  
151 the Arduino Uno microcontroller and two servo motors.

#### 152 **4.1.1 Light Dependant Resistor**

153 Light dependant resistor (LDR) or Cds photocell shown in Fig. 5-a composed of  
154 a high resistivity semiconductor, is a component whose resistor value decreases  
155 exponentially when the sunlight intensity (illumination in *lux*) increases as shown in  
156 Fig. 5-b. This intensity of light sensed by the LDR is used as analog input voltage to the  
157 ATMEGA microcontroller.

158 For our application, we use four identical LDR in a lunette disposed in cross on  
159 the panel surface and optically isolated by an opaque plate as shown in Fig. 5-c, so that  
160 their illumination are similar only if the lunette is pointed toward the sun.

161 This lunette is fixed on PV panel and placed on the same plan. These form a sensor  
162 designed to detect the sun position. A signal error is generated if the system is none  
163 pointed. It is the signal which will be used by the microcontroller to deliver the  
164 adequate control to DC servo motors. To process this signal, we have used a voltage  
165 divider for each LDR.

166 The output voltage  $V_{out}$  is proportional to the light intensity.  $V_{out}$  will increase  
167 when the maximum light is captured by the LDR and  $V_{out}$  is weak when the LDR is in  
168 the shadow, expressed by:

$$169 \quad V_{out} = \frac{V_{in} \cdot R}{(R + R_{LDR})} \quad (1)$$

#### 170 **4.1.2 Servo motors**

171 The objective of servo motors is to provide an exact movement as a response to  
172 an external control. It is an actuator mixing electronic, mechanic and automatic. Servo  
173 motors high torque servo having very large power range, are available in a wide variety

174 of frame sizes from small to large, capable of running huge machines, have an excellent  
175 power to weight size ratio given their best efficiency (80-90%), will do fine with low  
176 speed applications given low friction and the correct gear ratio leading to a very low  
177 heat production, vibration and very little noise.

178 The servo motor in [Fig. 6](#) is an assembly of three basic blocks, a body  
179 comprising all the mechanics and the electronics, a cable to lead power and the control  
180 (reference signal), a pioneer attached to the servo motor axis. We attach on the pioneer  
181 the mechanic parts to move (arm, wheel...).

182 This type of servo motor requires regulated supply voltage of 5V. This consists  
183 of three wires namely signal, positive and ground wire.

184 It also comprises several internal parts which are the motor and gearbox,  
185 position sensor, an error amplifier, motor driver and a circuit to decode the requested  
186 position. Servo motor only rotates by the maximum of *180 degrees*.

### 187 **4.1.3 The servo motor internal constitution**

188 The servo motor used in this project is an assembly of four parts: an electrical  
189 DC motor, a gearbox, a position-sensing device which is usually a potentiometer and an  
190 electronic card to control and assess motor.

191 The servo motor body is composed of an electronic card receiving the reference  
192 signal to realize assessment. This card controls an electrical DC motor which will drive  
193 the pioneer through the speed-reducing gear as illustrated in the following [Fig. 7](#).

194 The gearbox has two functions:

195 - Reducing the speed to provide an accurate tracking of relative position of the servo  
196 motor and to avoid damage of the system when movement is driven by its speed if it is  
197 very high.



198 - Increasing the torque by its mechanical movement of rotation. At an instant  $t$ , if we  
199 decrease the speed  $\Omega$  leaving the same mechanical power  $P_{mec}$ , this will increase the  
200 torque  $T$ .

201 **Fig. 8** shows a DC servo motor responses of rotating speed via supplying  
202 voltage  $\Omega=f(U)$ , electromagnetic torque via armature current  $T=f(I_a)$  and torque via  
203 angular speed  $T=f(\Omega)$ .

204 Speed is related to supplying voltage and current is related to the  
205 electromagnetic torque. Hence for a given fixed speed, if our system must increase the  
206 mechanical power to move a heavier load (solar panel weight), this will increase current  
207 (knowing that  $U$  and  $\Omega$  remain constant and electrical power  $P_{el}=U.I$ , must be equal to  
208 mechanical power  $P_{mec}=T.\Omega$ , when all internal losses are neglected). Since consumed  
209 energy by the system is generated by the panel itself, to improve efficiency, power  
210 consumption of the solar tracker is reduced since the servo motors supply the amount of  
211 torque just sufficient to move it (its mass is about 250 g).

212 **Fig. 8-a** shows the angular speed  $\Omega$  of the servo motor changed with the output  
213 voltage  $U$  of the drive unit. The speed  $\Omega$  starts obviously at zero (servo motor at rest) to  
214 reach its maximal value 7.8 rad/s. We observe that  $\Omega$  increases in a linear manner with  
215 voltage  $U$  to stabilize at an approximate specific value for 5V.

216 **Fig. 8-b** shows evolution of torque  $T$  via current  $I$ . The drive unit controls the  
217 output torque linearly, starting at  $T_L= 16.3 \text{ kg cm}$ , to increase with current.

218 **Fig. 8-c** shows evolution of  $T$  via  $\Omega$ . We notice that the servo motor keep its  
219 torque value even when its speed increases, but when the motor reaches its nominal  
220 speed of 7.7 rad/s; servo motors supply the amount of torque 10 kg.cm just sufficient to  
221 move it.

## 222 **4.2 Servo motor working**

223 PWM is used to control the motors. PWM analog signal will go through an  
224 electronic circuit and convert the analog signal into a digital signal. PWM in servos is  
225 used to control the direction and position of the motor. There were two servo motors  
226 used in this project for horizontal and vertical axis respectively.

227 Servo motors are controlled using an electrical cable composed of three wires to  
228 supply the motor (positive and ground) and the third one is used to transmit a PWM  
229 analog signal to control the motor positions. This means that it is the period of  
230 impulsions which determine the absolute angle of the output axis and then the position  
231 of the control shaft of servo motor. The signal is periodically repeated, in general every  
232 20 milliseconds as shown in [Fig. 9](#). This permits electronics to control and continuously  
233 correct the output axis angular position. This one is measured by the potentiometer.  
234 When the servo motor rotates, axis of servo motor changes the position that will modify  
235 the potentiometer resistance. The role of the electronic circuit is to control the motor so  
236 as output axis position will be conform to the received reference signal: it is  
237 an assessment.

## 238 **5. Microcontroller and Programming**

239 Our active sun tracker is controlled by PC program using an Arduino Uno. In  
240 this section, we will present the specifications of the microcontroller and the developed  
241 programming to conduct the exact system working.

### 242 **5.1 The microcontroller**

#### 243 **5.1.1 Advantages of the microcontroller**

244 The use of microcontrollers for programming circuits posses various strong and  
245 real advantages. Actually, we find the spectacular evolution of IC (Integrated Circuit)  
246 design in recent years.

247 It encompasses various components decreasing the cumbersomeness of materials  
248 and IC, simplifying the tracing of printed circuits to drive data bus address, increasing  
249 system reliability and reducing cost.

### 250 **5.1.2 Microcontroller role in a solar tracker system**

251 The microcontroller converts analog signal captured from LDR to digital signal  
252 which will be compared to a tolerance input signal, to be transmitted to the servo motors  
253 in order to move the PV panels where it can receive maximum sunlight.

### 254 **5.1.3 Microcontroller choice**

255 Many designers propose microcontrollers (Microchip, Atmel, Texas-Instrument,  
256 Free Scale, NXP, Cypress, etc...). Each one proposes various families of  
257 microcontrollers (PIC and dpPIC from Microchip; AVR, AVR32 and ARM from  
258 Atmel, etc...). Each family contains tens of models, which are basically different by  
259 their memories sizes and the I/O pins number.

260 The choice of microcontroller is done on the basis of application even it is  
261 preferable to fix a family. Even if the PIC microcontroller of Microchip have  
262 contributed to popularise the architecture reduced instruction set computer (RISC), so  
263 much in the world of microcontrollers as well in the literature devoted to informatics  
264 architectures, there were not the only one circuits in the market. The microcontrollers of  
265 AVR family from Atmel, for which this paper have been dedicated, using this  
266 architecture and hence benefits various advantages.

267 The AVR family have a lot of advantages, cheap, low energy consumption, and  
268 a good support multi-platform. They are successful, given these specifications:

269 Good: they work well. They are easy to program in C++ language for the most basic  
270 functions. Adequate documentation exists.

271 Economic: A lot of pieces of 3–5 Euros, disposable from big distributors in small  
272 quantity.

273 Low energy consumption.

#### 274 **5.1.4 ATMEGA microcontroller**

275 The microcontrollers of the family ATMEGA, in technology CMOS, are models  
276 of *8 bits* AVR based on architecture RISC. When we execute instructions in a simple  
277 clock cycle, the ATMEGA realises operations reaching *1 MIPS by MHZ* allowing  
278 simple systems design and low energy consumption.

#### 279 **5.1.5 Structure of an ATMEGA microcontroller**

280 The ATMEGA328P microcontroller is featured by the following particularities:

- 281 ○ A Flash Memory of *32KB* for program storage.
- 282 ○ A SRAM Memory of *2KB* for variables storage.
- 283 ○ An EEPROM Memory *1KB* for permanent robot parameters storage.
- 284 ○ Technology RISC (one instruction per clock cycle) which confer a power of *20*  
285 *million instructions per second* (MIPS) for a clock frequency of *20 MHz*.
- 286 ○ Include an UART (universal asynchronous receiver/transmitter) compatible RS232  
287 for the communication with the PC.
- 288 ○ Include I2C Bus for the communication with the components I2C.
- 289 ○ An Analog/Digital converter ADC of *6 channels of 10 bits*.
- 290 ○ Supplying voltage of *2.7 V to 5.5 V*.

#### 291 **5.1.6 Synopsis**

292 [Fig. 10](#) shows the synopsis of the internal hardware architecture of the  
293 ATMEGA328P microcontroller:

#### 294 **5.1.7 Pins description**

295 It is an IC of 28 pins dual in line shown in Fig. 11, where 14 are digital  
296 input/output of which 6 provide PWM outputs, 6 analog inputs, a 16MHz quartz crystal  
297 oscillator, an ICSP (In Circuit Serial Programming) header, an USB connection, a  
298 power jack and a reset button.

- 299 ○ VCC: supplying voltage (+3V to +5V).
- 300 ○ GND: ground.
- 301 ○ Port B (PB7... PB0): it is bidirectional I/O port of 8 bit with internal pull-up resistors  
302 chosen for each bit.
- 303 ○ PB6/XTAL1: External Oscillator amplifier input or free for internal clock.
- 304 ○ PB7/XTAL2: Output of the Oscillator amplifier.
- 305 ○ Port C (PC5 ... PC0): it is bidirectional I/O port of 7 bit with internal pull-up resistors  
306 selected for each bit.
- 307 ○ PC6/ RESET: Released by falling front maintained for more than 50ns producing the  
308 reset of microcontroller, even if the clock is at rest.
- 309 ○ Port D (PD7 ... PD0): The D port is bidirectional I/O port of 8 bit with internal pull-  
310 up resistors chosen for each bit. It is used so as USART and inputs for external  
311 interruptions.
- 312 ○ AVcc: It is supplying voltage pin for the A/D converter which must be connected to  
313 Vcc via low pass filter to avoid parasites.
- 314 ○ AREF: It is the analog reference input for the A/D converter with a voltage of 2 V to  
315 AVcc with low pass filter.

### 316 **5.1.8 Oscillator**

317 The external quartz crystal oscillator is connected on XTAL1, XTAL2 as shown  
318 in Fig. 12 to cadence the microcontroller. Crystal type Quartz frequency is from 4 to 16  
319 MHZ or ceramic resonator.

320 Using the external quartz oscillator, a capacitive damper of about  $12$  to  $22$   $pF$   
321 must be connected as shown in Fig. 12 here up.

### 322 5.1.9 A/D Converter (ADC)

323 The Analog to Digital Converter integrated in the ATMEGA is doted of very  
324 interesting specifications with  $10$  bit resolution, 6 simultaneous inputs. This ADC  
325 converts analog voltage to digital signal coded on  $10$  bit described by resolution  
326 equation (2):

$$327 \text{ Resolution} = \left( \frac{V_{in}}{V_{A.ref}} \times 1024 \right) - 1 \quad (2)$$

## 328 5.2 Design of the solar tracker control circuit

329 A dual axis tracker based on four identical LDRs was constructed and tested to  
330 set the optimal values of the potentiometers  $R_{VIT}$  and  $R_{TOL}$  shown in both Fig. 3 and  
331 Fig. 13. The  $R_{TOL}$  tolerance was calculated in terms of the angle between the up side  
332 couple of (LDR1, LDR3) and down side couple of (LDR2, LDR4) sensors. After  
333 some initial and trial error testing, the optimal angle between these photo-resistors  
334 was evaluated experimentally to set the tolerance voltage value  $TOL$ . Precise results  
335 have been found because the system is working in close-loop system. This latter using  
336 photo sensors is the conventional control method of sun tracking systems. The photo  
337 sensors are used to discriminate the sun's position and then sending the proper analog  
338 electrical signals, converted to digital signal, proportional to controller error, which  
339 actuates the motors to track the sun [17], [28]. Circuit scheme of the designed system  
340 for horizontal and vertical axis is shown in Fig. 13. When the sun moves to the east or  
341 to the west, either the couple (LDR3, LDR4) or (LDR1, LDR2) will get more light,  
342 transforming the solar light intensity collected to electrical voltages  $V_{LDR3,4}$  or  $V_{LDR1,2}$   
343 using the voltage dividers (Equ.1). These latter are sent to ADC ports ( $Pc_0$ ,  $Pc_1$ ) for  
344 the altitude angle or ports ( $Pc_2$ ,  $Pc_3$ ) for the azimuth angle tracking, to the  
345 microcontroller for comparison with the tolerance input signal  $TOL$  sent to ADC port  
346 ( $Pc_5$ ), to control servo motors. These ones are acting the orientation of the PV panel  
347 towards the sun. Rotation directions for the azimuth and altitude angles tracking  
348 respectively the horizontal (H) and vertical (V) motors are controlled by using two

349 differential amplifiers (op-amp-H, op-amp-V). Couples ( $V_{LDR3,4}$ ,  $V_{LDR1,2}$ ) and ( $V_{LDR1,3}$ ,  
350  $V_{LDR2,4}$ ) voltages are sent to the microcontroller for average computation and  
351 comparison with  $TOL$ . According to the average differences between the voltages  
352 from LDR couples  $d_{vert} = |mean(V_{LDR1,3} - V_{LDR2,4})|$  or  $d_{horiz} = |mean(V_{LDR1,2} -$   
353  $V_{LDR3,4})|$  are bigger or smaller than the fixed value  $TOL$ ; the proper logic signals are  
354 sent to the errors op-amps to drive the DC motors. The width of PWM control signal  
355 shown in Fig. 9, generated by using AVR timers, determines the absolute angle of the  
356 output axis and then the position of the control shaft of servo motors. When the  
357 motors rotate, H and V axis change the positions that will accordingly modify the  
358 potentiometers resistances (position sensors of the assessment electronic card in Fig.  
359 7) mounted on the shafts and provide the H and V feedback voltages. These ones will  
360 be compared to PWM control signals to determine the positions of the DC motors.  
361 Finally, H-motor and V-motor are turned in such directions clockwise (cw) or  
362 counter-clockwise (ccw) that the absolute values of  $d_{horiz}$  and  $d_{vert}$  become less  
363 than the  $TOL$  value and the motors are then stopped. When the light sensors have the  
364 same amount of resistance values (i.e. for the same rate of light), the error amplifiers  
365 give the same output (0 V) (i.e. the lunette in Fig. 5-c is pointed towards the sun) and  
366 since the potential difference at the motor terminals is zero, the panel does not rotate.

367 We have used the logic ISIS Proteus for the simulation of our montage in Fig.13.  
368 We present the assemblage of different parts of the system, before mentioned on the  
369 global electric scheme of the installation represented as follow:

370 We set the optimal value of potentiometer  $R_{VIT}$  depending on the weight of the  
371 PV panel. For our system we fixed  $R_{VIT}$  to  $2.5 k\Omega$ .

372 If we choose a very small value of the tolerance, for example  $TOL=0.0001V$ ; our  
373 panel will oscillate. The potentiometer  $R_{TOL}$  will be taken so that the difference is with a  
374 tolerance of  $0.5V$  for a proper working of our system.

### 375 **5.3 Developing Environment**

376 We have chosen the compiler gcc-avr which is compatible with most popular  
377 platforms (Windows, Linux and Mac).

378           To transmit the software PC program to the Atmega328p microcontroller, we  
379 must use conversion USB series module, it is the FTDI Basic Breakout in the same card  
380 comporting a microcontroller noted Arduino Uno.

381           Arduino Uno developing environment is a Java multi-Platform application, used  
382 as code editor and compiler, to transmit code to asynchronous serial liaison using C++  
383 programming language.

384           The Atmega328P pin mapping with Arduino Uno board is shown in [Fig. 14](#) for  
385 its programming using C++ language in [Appendix A](#).

386

### 387 **// C++ Program compilation**

```
388 #include <Servo.h> // include Servo library. Include the class of Servo.h, allow for easily manipulating
389                 the complete management of servo motor
390
391 Servo horizontal; // horizontal servo. Create "initialize the object servo"
392 int servoh = 90; // stand horizontal servo
393
394 Servo vertical; // vertical servo
395 int servov = 90; // stand vertical servo
396
397 // LDR pin connections
398 // name = analogpin;
399 int ldr1t = 0; //LDR top left
400 int ldr1r = 1; //LDR top right
401 int ldr1l = 2; //LDR down left
402 int ldr1d = 3; // LDR down right
403
404
405 void setup()
406 {
407     Serial.begin (9600);
408     // servo connections
409     // name.attach(pin);
410     horizontal.attach(9);
411     vertical.attach(10);
412 }
413
414 void loop()
415 {
416     int lt = analogRead(ldr1t); // top left
417     int rt = analogRead(ldr1r); // top right
418     int ld = analogRead(ldr1l); // down left
419     int rd = analogRead(ldr1d); // down right
420
421     int dtime = analogRead(4)/20; // Read potentiometers
422     int tol = analogRead(5)/4;
423
424     int avt = (lt + rt) / 2; // Average value top
```



```

424 int avd = (ld + rd) / 2; // Average value down
425 int avl = (lt + ld) / 2; // Average value left
426 int avr = (rt + rd) / 2; // Average value right
427 int dvert = avt - avd; // Check the difference of up and down
428 int dhoriz = avl - avr; // Check the difference of left and right
429
430 if (-1*tol > dvert || dvert > tol) // Check if the difference is in the tolerance else change vertical angle
431 {
432     if (avt > avd)
433     {
434         servov = ++servov;
435         if (servov > 180)
436         {
437             servov = 180;
438         }
439     }
440     else if (avt < avd)
441     {
442         servov = --servov;
443         if (servov < 0)
444         {
445             servov = 0;
446         }
447     }
448     vertical.write(servov);
449 }
450
451 if (-1*tol > dhoriz || dhoriz > tol) //Check if the difference is in the tolerance else change horizontal angle
452 {
453     if (avl > avr)
454     {
455         servoh = --servoh;
456         if (servoh < 0)
457         {
458             servoh = 0;
459         }
460     }
461     else if (avl < avr)
462     {
463         servoh = ++servoh;
464         if (servoh > 180)
465         {
466             servoh = 180;
467         }
468     }
469     else if (avl = avr)
470     {
471         // nothing
472     }
473     horizontal.write(servoh);
474 }
475     delay(dtime);
476 }
477
478

```

**Appendix A. Tracking control C++ Program.**

## 479 **6 Various steps of the mechanical design**

480 In this section, we will design the mechanical parts adopted for the solar tracking

481 mode working on the basis of horizontal and vertical directions of varying angle  
482 respectively from  $0^\circ$  to  $180^\circ$  and from  $0^\circ$  to  $90^\circ$ . The mechanical design consists of  
483 rotary joints and two DC servo motors.

#### 484 **6.1 Photovoltaic panel prototype**

485 [Fig. 15](#) shows our design as a prototype composed of wood plate. Its size is  $460$   
486  $\times 285$  mm and its mass is about  $250$  g. This woody plate will be fixed by seven vices in  
487 seven points on the vertical axis; three in front and four behind.

#### 488 **6.2 The lunette**

489 [Fig. 16](#) shows the lunette which is fixed to the photovoltaic panel prototype and  
490 placed on the same plan. It is composed of four LDR disposed in cross and optically  
491 isolated from each others, leading at a such way that the light intensity will not be  
492 identical only if the lunette is pointed towards the sun.

#### 493 **6.3 Vertical axis**

494 Vertical axis is realized in wood of size  $390$  mm each side. Dual ball bearing  
495 facilitates their rotation. [Fig. 17](#) shows how we have fixed the servo motor HS-  
496 645MG standard deluxe in one side.

#### 497 **6.4 Horizontal axis**

498 It is realized in such a way that ball bearing will be in the middle of the axis as  
499 shown in [Fig. 18](#), in order to be able to drive the sole.

#### 500 **6.5. The basis**

501 It is realized in wood of size  $390 \times 390$  mm as shown in [Fig. 19](#). Its role is to  
502 insure the assize and the stability of the installation.

503 To orient the panel towards the solar rays, we must first of all, make the choice  
504 of the motors.

505 The size of the prototype tracker panel is imposed by the torques of servo

506 motors. These constraints have conducted to the design of an experimental tracker  
507 where the quotations are mentioned on the [Fig. 20](#) hereunder ( $340mm \times 275mm$ ):

## 508 **7 Management of system flowchart**

509 The global program intended to a programmable circuit, is based on a well  
510 precise idea to satisfy the constructor catalogue and industrial context. This one is  
511 generally translated through a flowchart defining the various steps of the program.

### 512 **7.1 Basic software design**

513 The basic software flowchart of the solar tracker system is illustrated in  
514 [Appendix. B](#) as follow:

515

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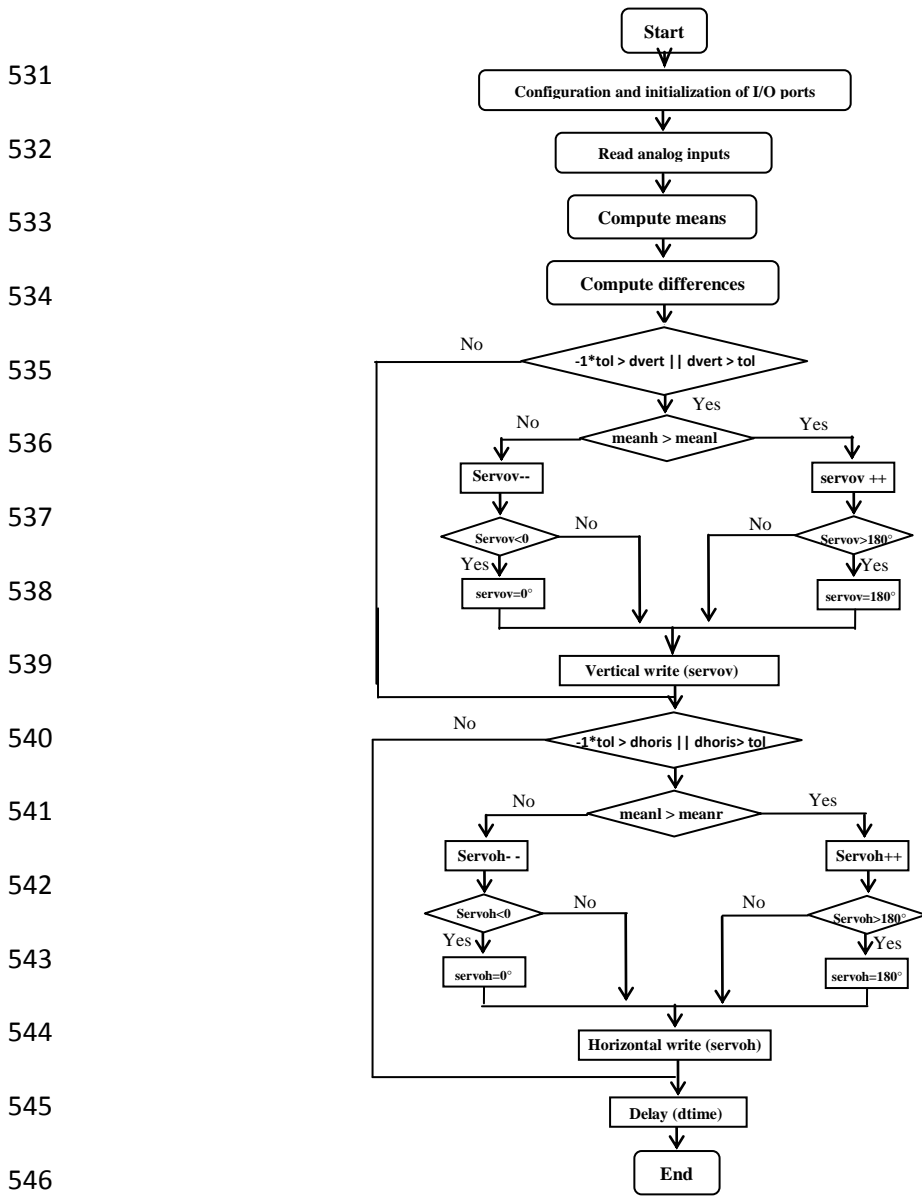
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530



547 **Appendix B.** Tracking control flowchart.

548 **7.2 Explanation of the flowchart**

549 We begin by configuration and initialization of I/O ports.

550 It is the nomination of the type of configuration of inputs or outputs ports indicating the  
 551 used pins.

552 LDRlt = 0; ➔ LDR top left

553 LDRrt = 1; ➔ LDR top right

554 LDRld = 2; ➔ LDR down left

555 LDRrd = 3; ➔ LDR down right

556 Initialize the object servo

557 servoh = 90 degrees; → Stand horizontal servo

558 servov = 90 degrees; → Stand vertical servo

559 to have the panel in its vertical position when supplying the system.

560     ○ *Read the analog inputs*

561 We acquire and convert the analog signal to digital the values captured by the sensors.

562     ○ *Compute the mean values (means)*

563 Compute the means values for each couple of LDR among the four sensors illustrated in

564 [Fig. 13](#), as follow:

565 Between LDR1 and LDR3 → Mean value of the up side

566 Between LDR2 and LDR4 → Mean value of the low side

567 Between LDR1 and LDR2 → Mean value of the left side

568 Between LDR3 and LDR4 → Mean value of the right side

569     ○ *Compute the difference values (Diffs)*

570 - Compute the difference between the mean value of the up and low sides, to control the

571 vertical motor.

572 - Compute the difference between the mean value of the left and right sides, to control

573 the horizontal motor.

574     ○  $-1*tol > dvert \ || \ dvert > tol$

575 The previous obtained result «Compute diffs » will be compared to TOLERANCE

576 input signal (tol.). If we obtain an equal value, the motor is at rest; otherwise if we have

577 a different value the motor will move to change vertical angle.

578     ○  $meanh > meanl \ ; \ (h :high ; l :low)$

579         It will be the values of the vertical which permit to correct the vertical system

580 position. The motor will move the panel toward the side where there is a big value, but

581 when reached angle is 180° or 0°, the motor stops.

582       ○  $-l * tol > dhoriz // dhoriz > tol$

583           The previous obtained result « Compute diffs » will be compared to  
584 TOLERANCE input signal (tol.). If we obtain an equal value, the motor is at rest;  
585 otherwise if we have a different value the motor will move to change horizontal angle.

586       ○  $meanl > meanr$  ;           ( $l : left ; r : right$ )

587           It will be the values of the horizontal which permit to correct the horizontal  
588 system position. The motor will move the panel toward the side where there is a big  
589 value, but when reached angle is  $180^\circ$  or  $0^\circ$ , the motor stops.

590           Two delay times: short and long pauses.

591           The short pause is the delay of the position of the PV Panel relatively to the sun ray. We  
592 can fix a delay of 30 minutes to avoid wasting of energy, after which the panel change  
593 of inclination of 9 or 10 degrees following the new position of the sun.

594           The long mean pause of 12 h (from 10h to 15h depending on the season) will be  
595 at the end of the day, which permits to panels to have their initial positions.

## 596   **8 Conclusion**

597           The described program has satisfied the control conditions for the good working  
598 of the system so as results are encouraging. In fact, the program repartition permits to  
599 distinguish various realized operations. Instruction commented of the program guides in  
600 the methodical repairing of the functions. It facilitates the modifications which could be  
601 made during these works. The proposed montage uses a limited number of components,  
602 easy to use and occupy a restricted space which could be integrated in a complete  
603 photovoltaic system. The total cost reached only 150 Euros, and the period of  
604 realization is about 40 days. It has an effective contribution on the environment and  
605 could be improved. Two degrees of freedom orientation is made able to truck the sun  
606 position. In our case, we have tested the system using the flash-light of a moving

607 electrical lamp to shine it at the sensors; the tracker has been following it around, which  
608 was successful verifying its efficient and correct working. The microcontroller is used  
609 to control exact shaft position of DC servo motors which ensure point to point  
610 intermittent stable movement. The microcontroller is designed to rotate the panel from 0  
611 to 180 degrees. The presented dual axis solar panel tracking system keeps the solar  
612 photovoltaic panel perpendicular to the sun throughout the year to improve the  
613 efficiency of the system.

614 As advancements in photovoltaic trackers technologies have decreased  
615 investment prices, this project could be extended to power supply isolated villages or  
616 farms by mounting more optimal large and scheduled moving panels providing a huge  
617 solar energy. Scheduled tracking must use a computer program to change the angle of  
618 the panel based on date, time, and its physical location even under cloud coverage.

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732

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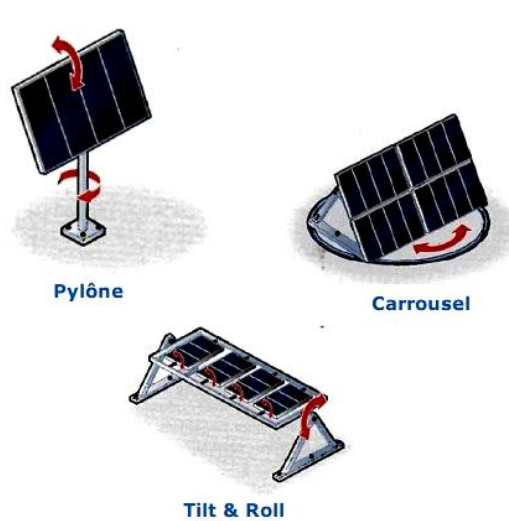
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764 **Table 1.**

zone	Coast zone	High planes zone	Sahara
Surface area (%)	4	10	86
Sunny mean period (hours/annum)	2650	3000	3500
Mean energy received (KWh/m <sup>2</sup> /annum)	1700	1900	2650

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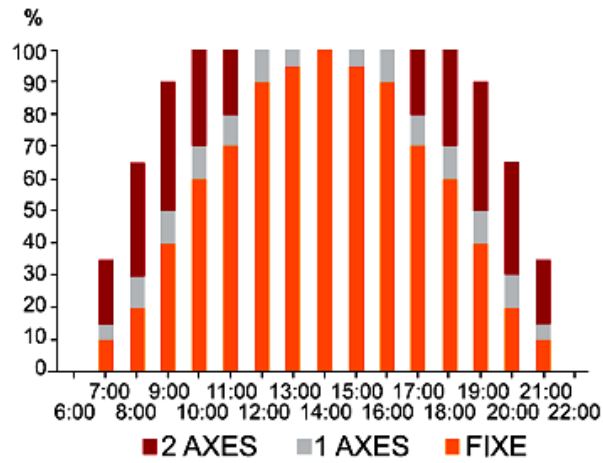
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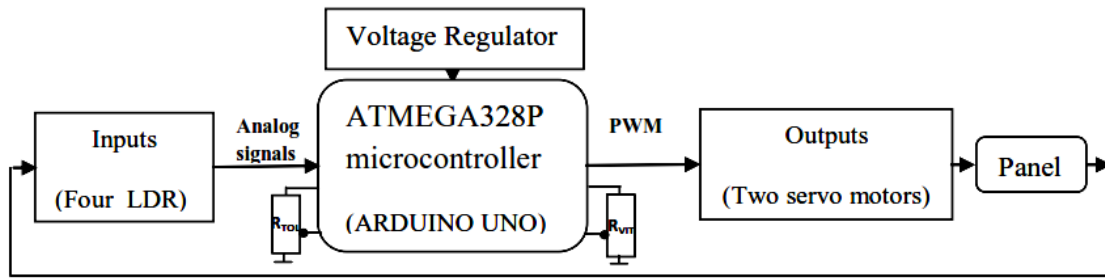
**Figure 1.**



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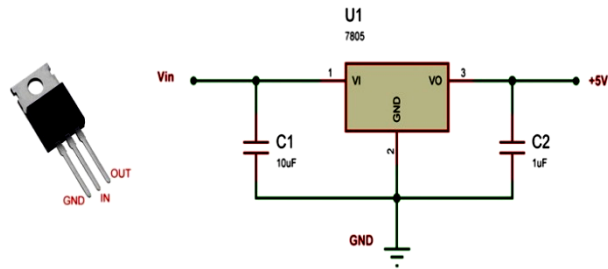
**Figure 2.**



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Figure 3.



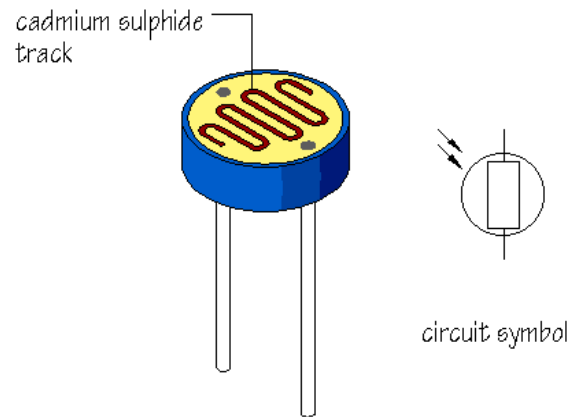
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Figure 4.

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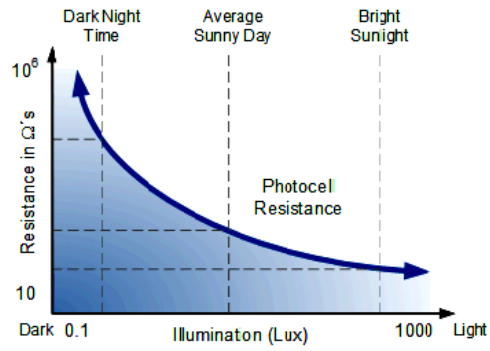
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Figure 5-a.

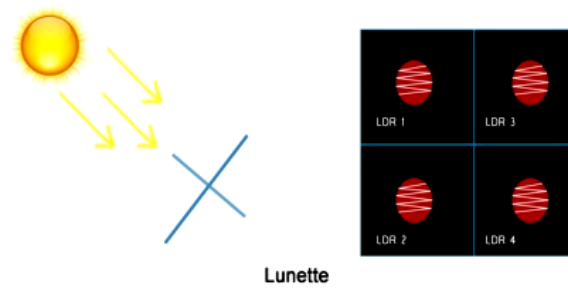


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Figure 5-b.

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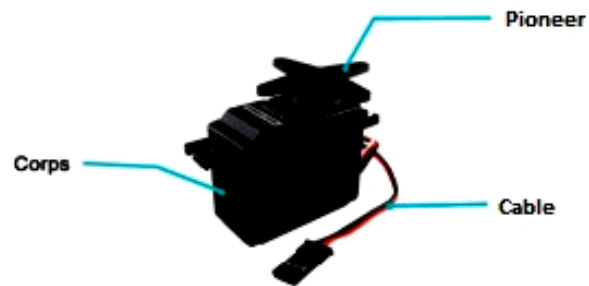
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Figure 5-c.

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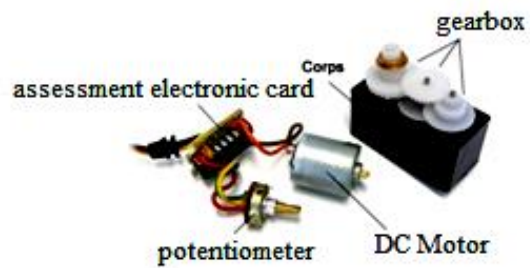
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Figure 6.

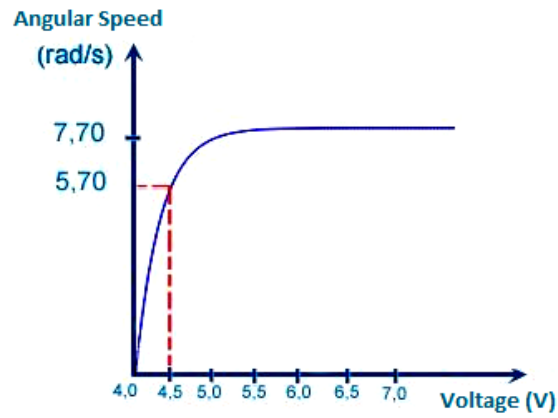
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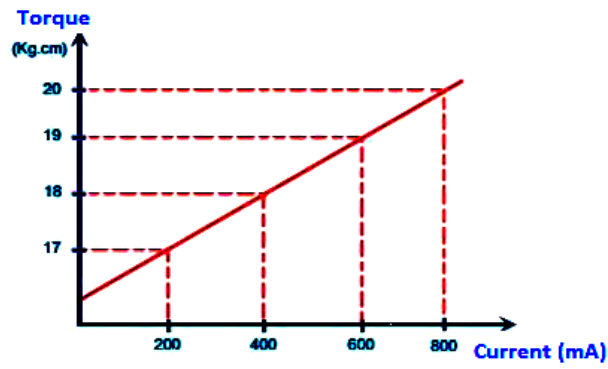
Figure 7.



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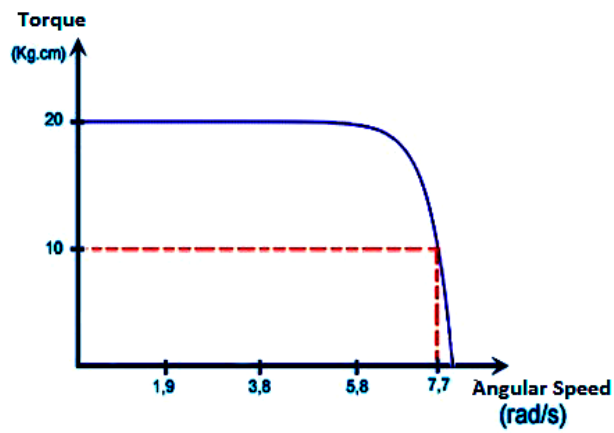
Figure 8-a.



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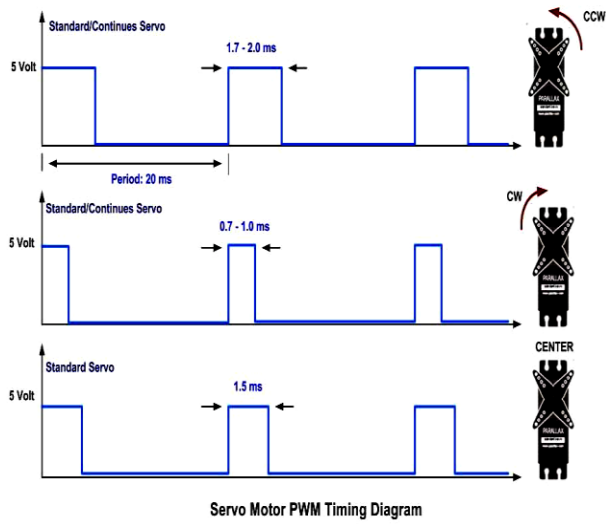
Figure 8-b.



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Figure 8-c.



Servo Motor PWM Timing Diagram

Figure 9.

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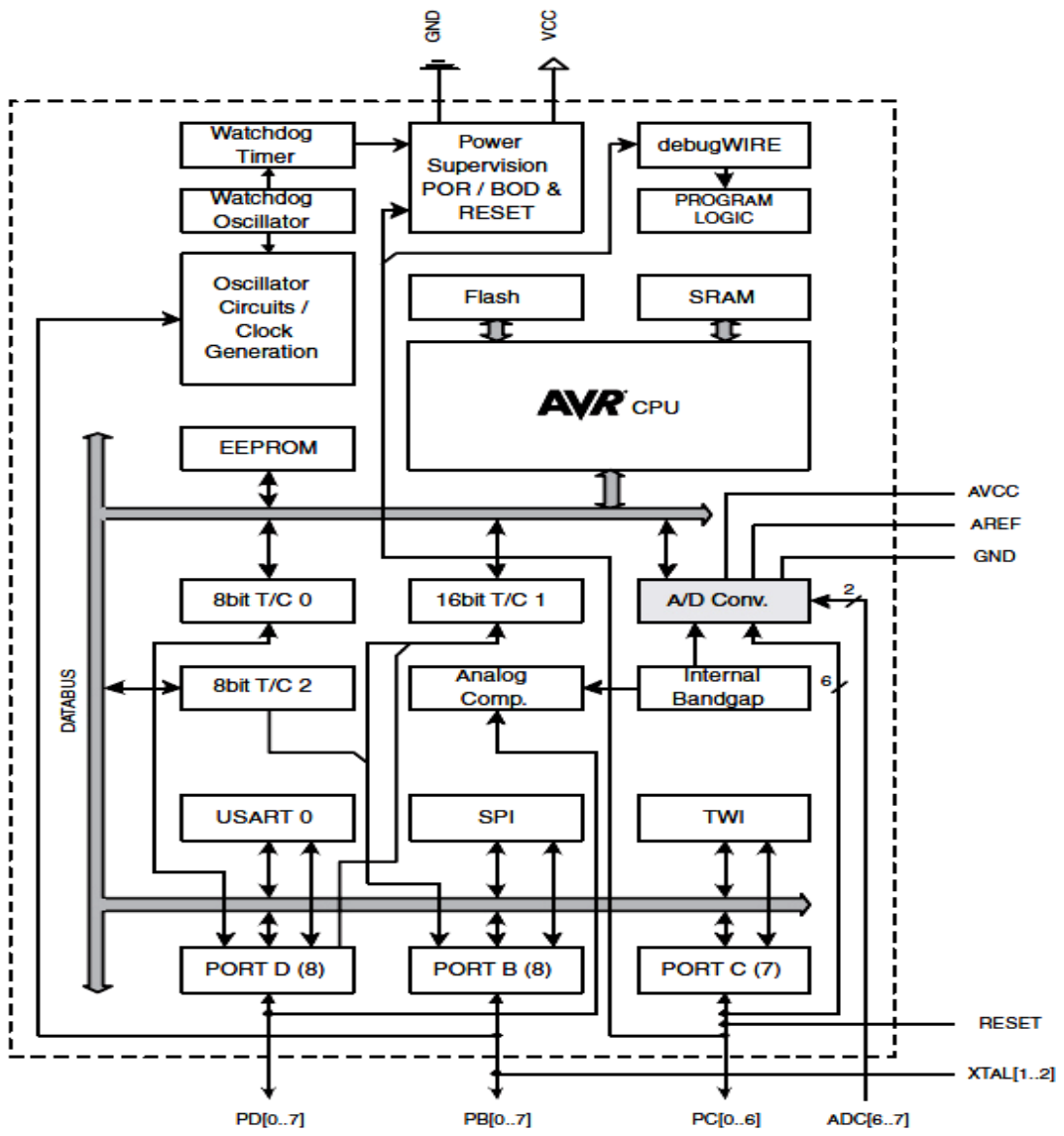
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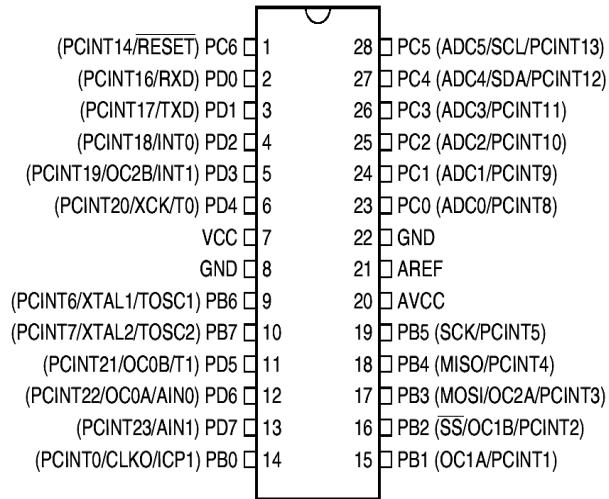
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Figure 10.

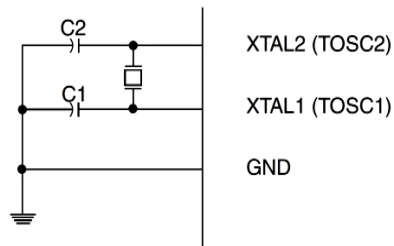


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**Figure 11.**



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**Figure 12.**

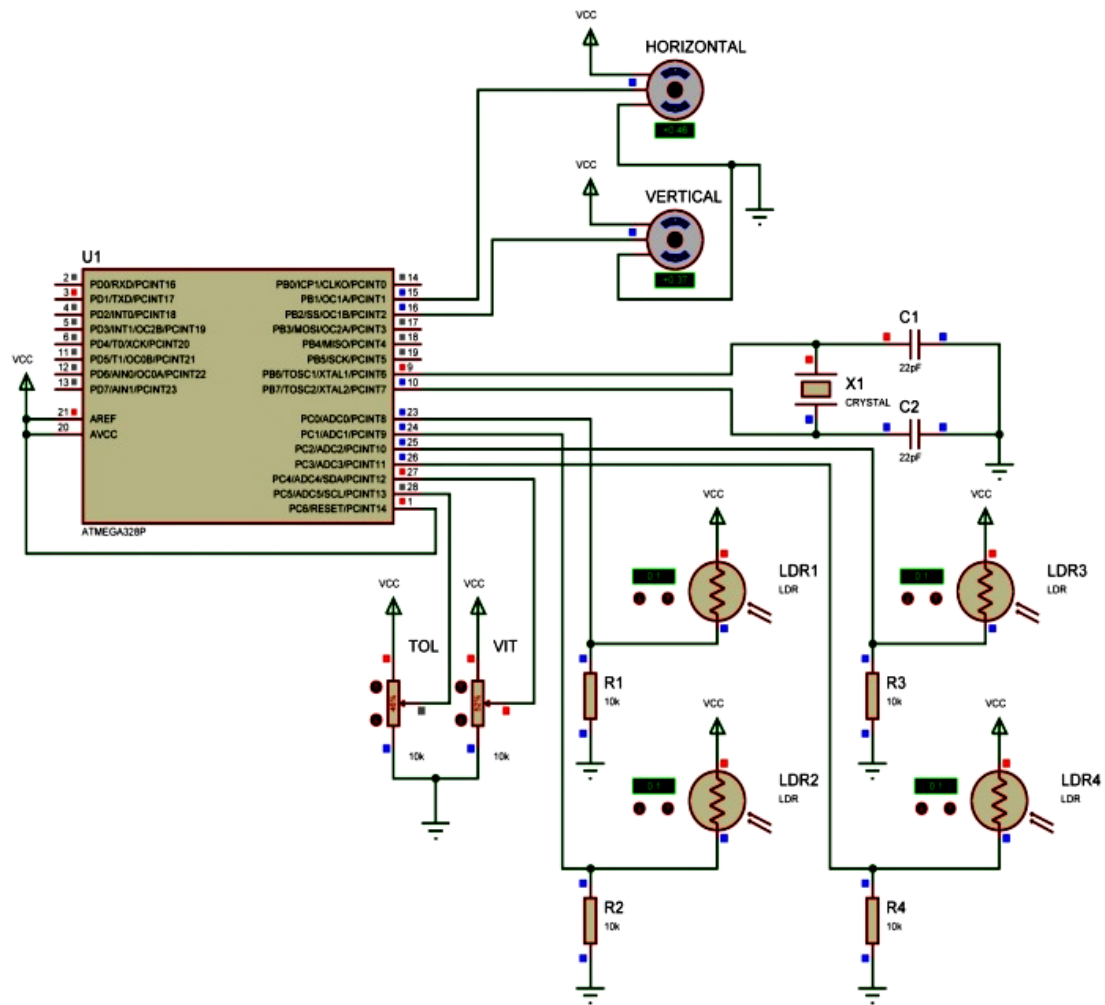


Figure 13.

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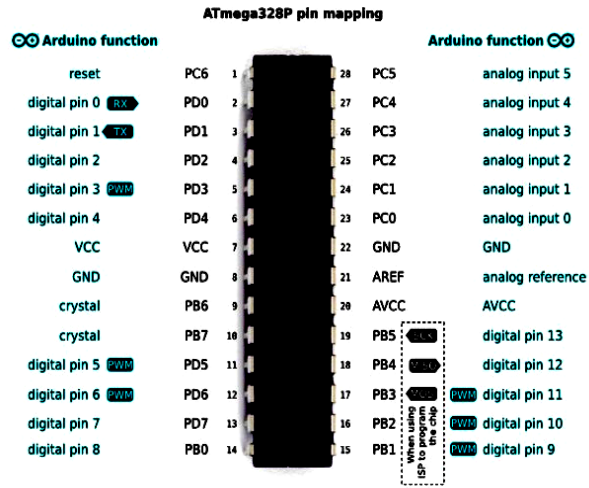
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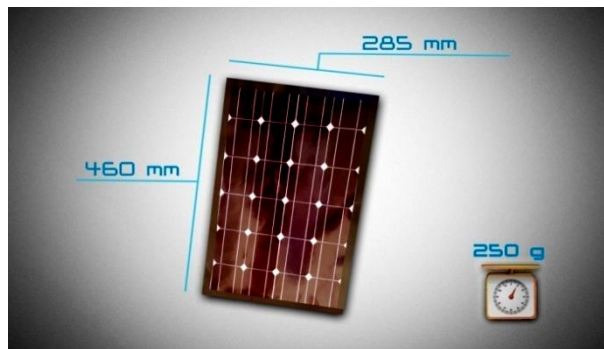
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Figure 14.



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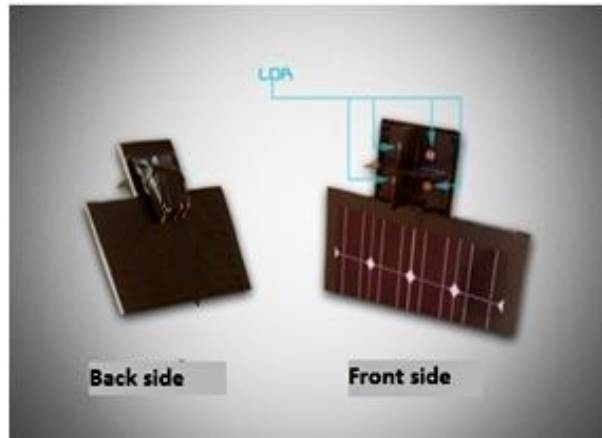
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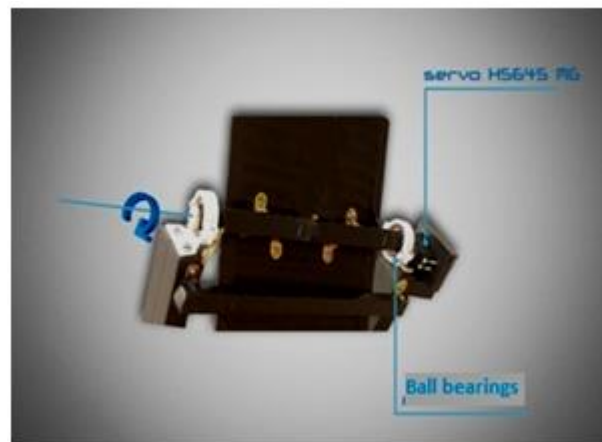
Figure 15.



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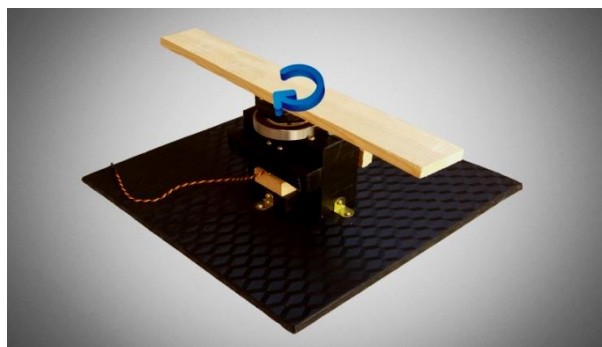
**Figure 16.**



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**Figure 17.**



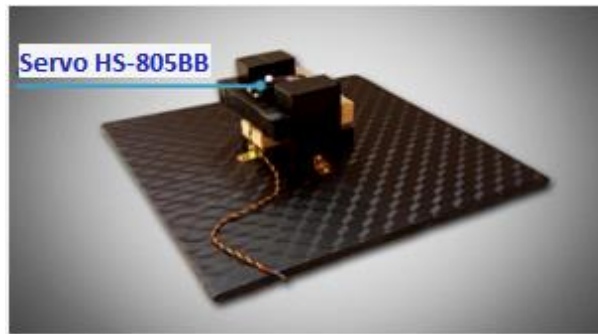
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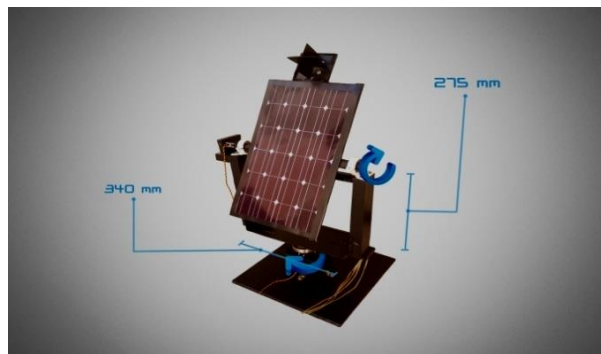
**Figure 18.**



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**Figure 19.**



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**Figure 20.**

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